

Doctoral School
ED184

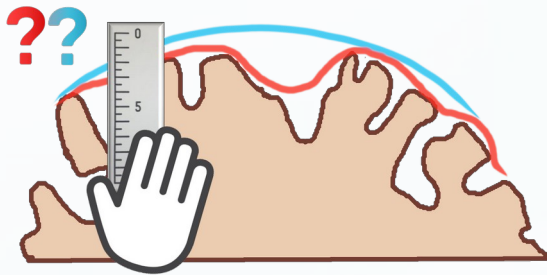
Computer Science - Mathematics

Size-controlled Sulcal Depth estimation

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How deep is your brain ?

Sulcal depth is a relevant descriptor and morphological feature to study :

- Methodological applications
- clinical applications

- exemples of methodological application : **Registration**

- (Robinson et al., 2017) Multimodal Surface Matching with Higher-Order Smoothness Constraints -> use of sulcal depth
- (Fischl, 2012) FreeSurfer -> registration based on SULC : sulcal depth estimation
- (Lyttelton et al., 2007) An unbiased iterative group registration template for cortical surface analysis -> based on sulcal depth

- exemples of **clinical applications** :

- (Li et al., 2021) Atypical sulcal pattern in boys with attention-deficit/hyperactivity disorder
- (Asschenfeldt et al., 2021) Abnormal Left-Hemispheric Sulcal Patterns in Adults With Simple Congenital Heart Defects Repaired in Childhood
- (Clouchoux et al., 2013) Delayed Cortical Development in Fetuses with Complex Congenital Heart Disease

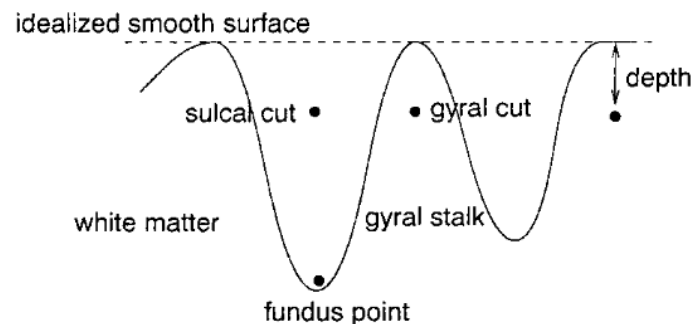
- exemples of methodological application/ **descriptiv surface development**

- (Bodin et al., 2021) Plis de passage in the superior temporal sulcus: Morphology and local connectivity
- (Leguen et al., 2018) Genetic Influence on the Sulcal Pits: On the Origin of the First Cortical Folds
- (Auzias et al., 2015) Deep sulcal landmarks: Algorithmic and conceptual improvements in the definition and extraction of sulcal pits
- ajouter im

► **The choice of sulcal depth method is critical for registration methods, clinical applications and description of the surface.**

- the intuition is simple, but practically not so easy : no clear definition
- top and bottom of fold : anatomical concepts
- no unique and formal geometric definitions for : gyri, fundi, wallpinches, valley, ridges ...

simple intuition

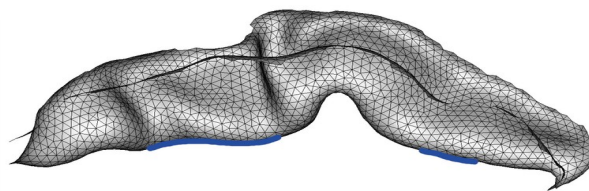


(Lohman et.al, 1998)

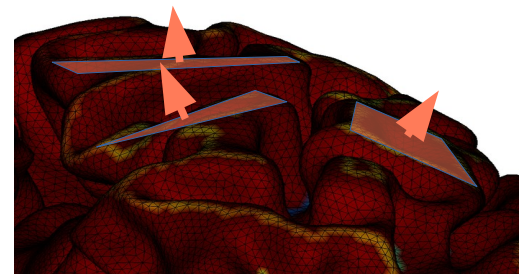
we want a reliable numeric method

OPEN QUESTION

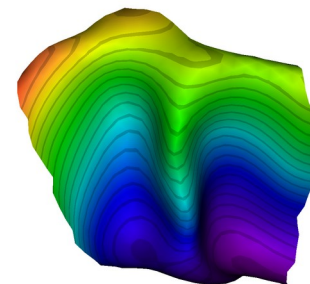
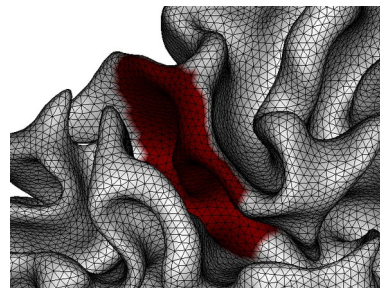
complex sulcal bassin



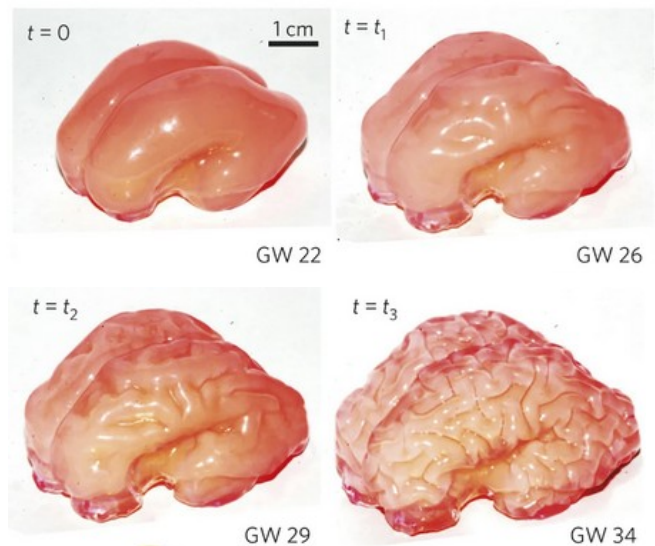
no clear extrema



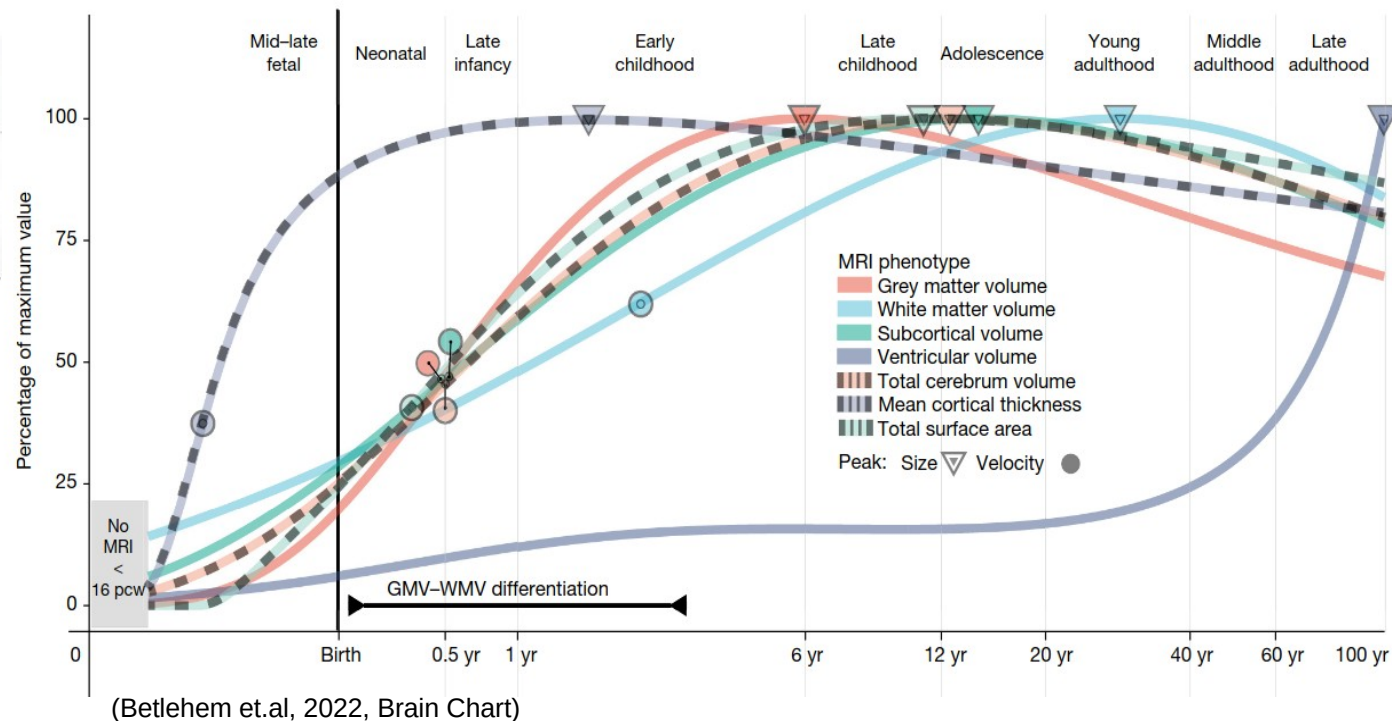
3D folding : buried gyri, Wallpinches ..



The folds and size change with age



(Tallinen et.al, 2016)



methods impact clinical results

1. What are the different sulcal depth estimation methods ?

Distance-based methods and their limits

Diffusion-based methods and their limits

2. How to evaluate the different methods ?

The methods are different

The differences impact your application

Literature : evaluation with clinical applications

Contribution : a framework for evaluate depth methods

3. How to deal with size variations of the brain ?

Literature : different methods for different size

Contribution : a unique size-controlled method

1. What are the different sulcal depth estimation methods ?

2. How to evaluate the different methods ?

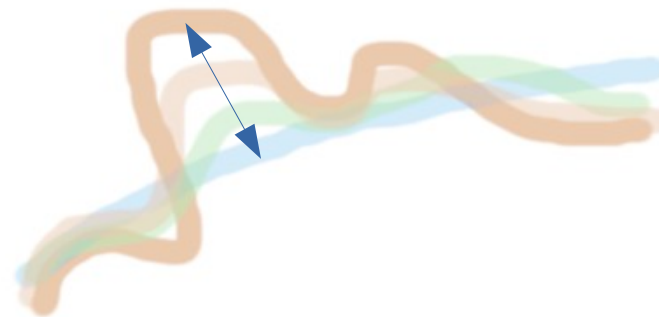
3. How deal with size variations ?

Distance-based methods



► Sulcal depth is the distance relative to an external surface

Diffusion-based methods



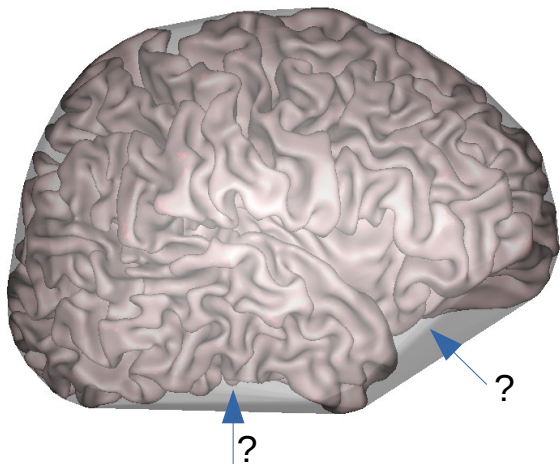
► Sulcal depth is estimated by a diffusion process

1.The different methods for sulcal depth estimations : distance-based

You need :

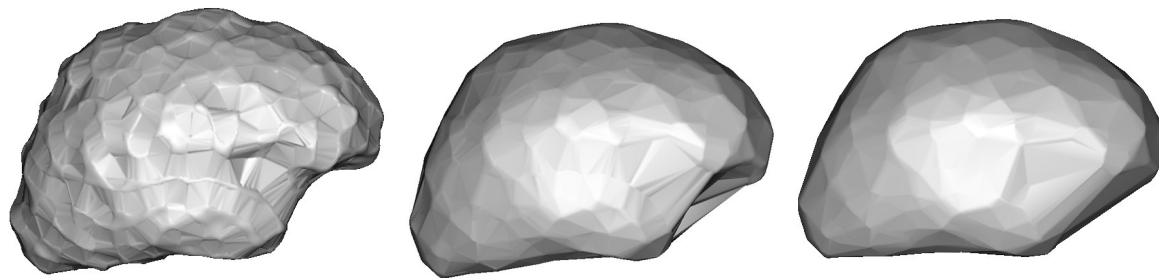
- **a distance definition** : Euclidean, Geodesic or Adaptive
- **an external surface** : Convex-hull or Alpha-shape/ Wrapper-surface

Convex-Hull



- unique definition
- but brain shape is not convex

Wrapper-Surface



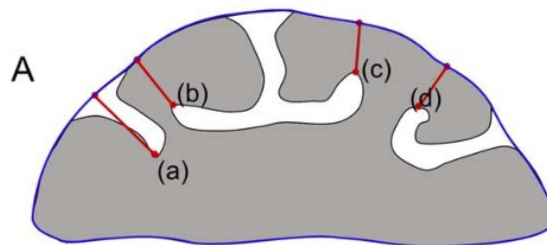
- adaptive to the convex/concav shape
- but no unique definition
- create artefacts
- require pre and post processings steps (smoothing, cleaning...)

1. The different methods for sulcal depth estimations : distance-based

You need :

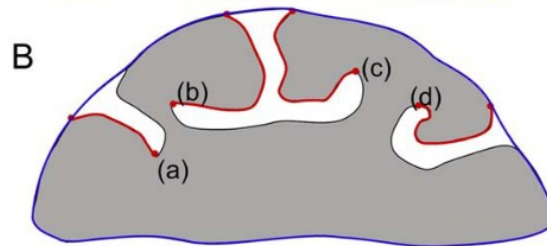
- **a distance definition** : Euclidean, Geodesic or Adaptive
- **an external surface** : Convex-hull or Alpha-shape/ Wrapper-surface

Euclidean distance



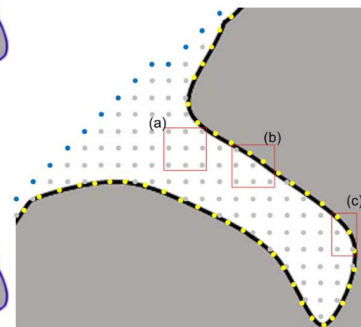
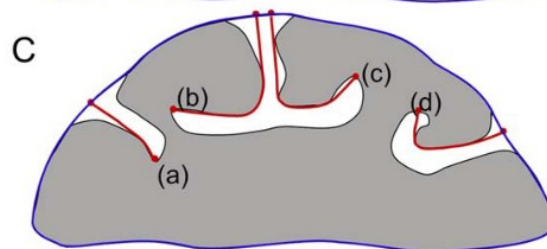
- underestimated high convoluted folds

Geodesic distance



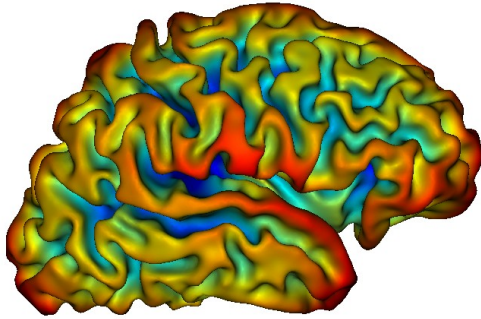
- overestimated shallow bassins

Adaptativ distance



- good alternative
- need to discretised the inbetween space
- noise sensitiv

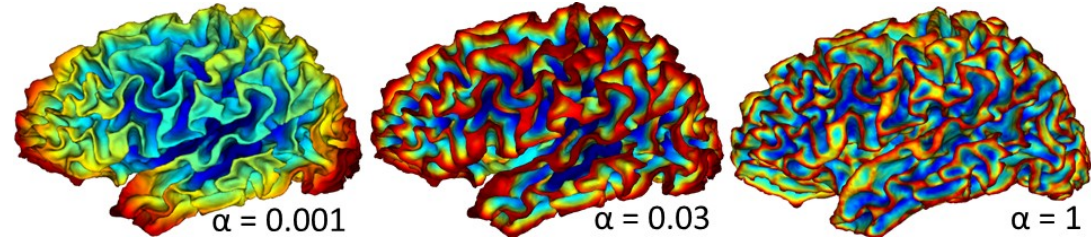
Sulc



from Freesurfer pipeline

(Fischl et.al, 2002)

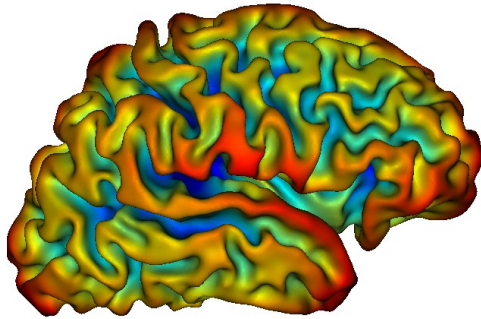
Depth potential function



based on a screened Poisson equation $(\alpha \cdot I + \Delta_M) D_\alpha = K$
facteur d'échelle laplacien profondeur courbure

(Boucher et.al, 2009)

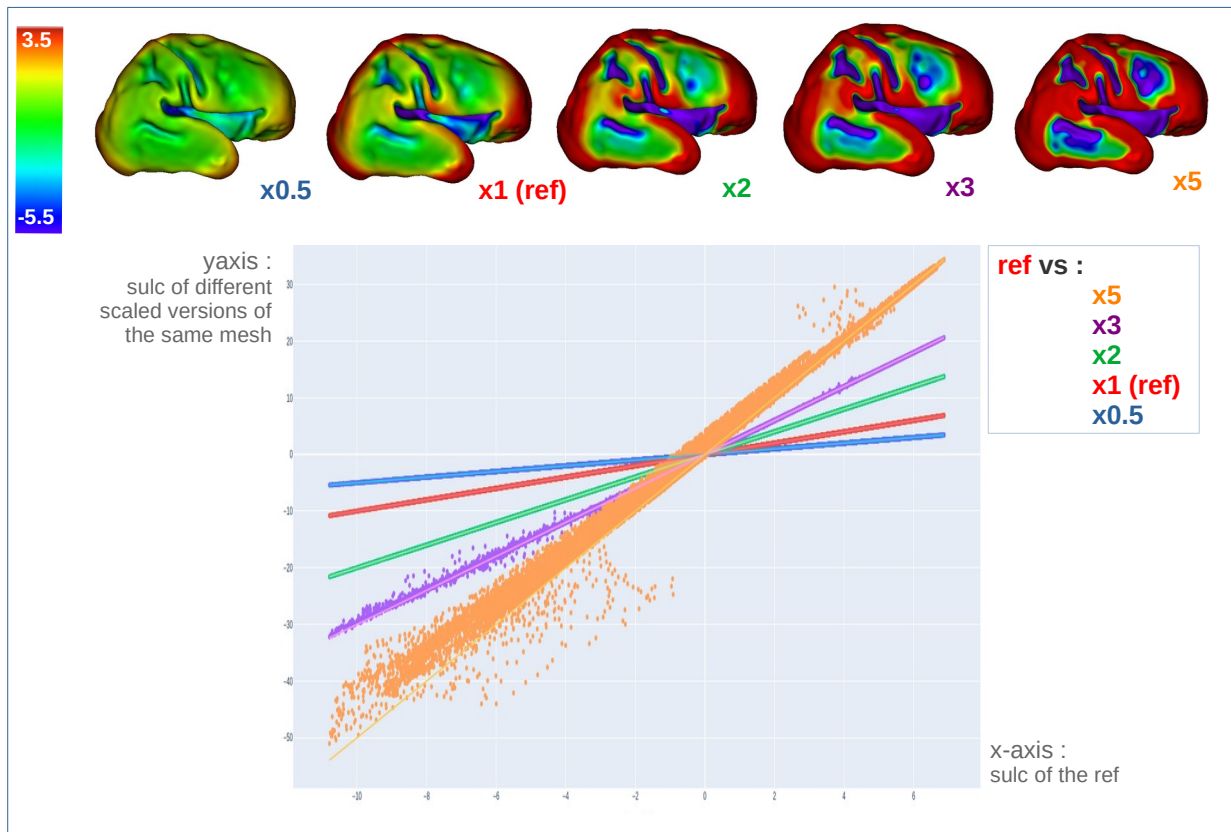
Sulc



from Freesurfer pipeline

- Depth is the distance travelled by each point during an inflation transformation of the mesh.
- kind of black-box, ready to use
- a lot of parameters and hyper parameters set by default
- method used a lot ! because easy to use.
- not robust to isometric scaling
- global and local inconsistencies for individual subject

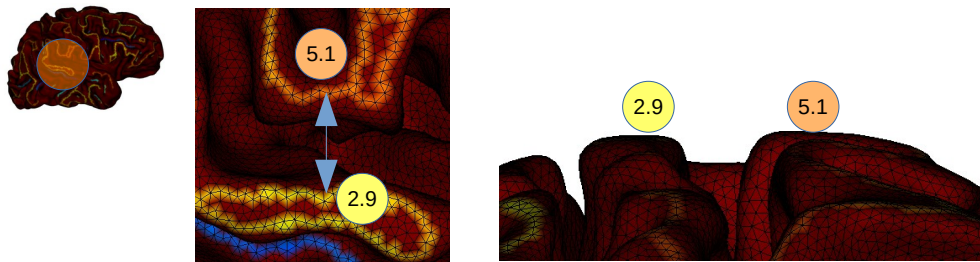
Not size invariant : not robust to isometric scaling



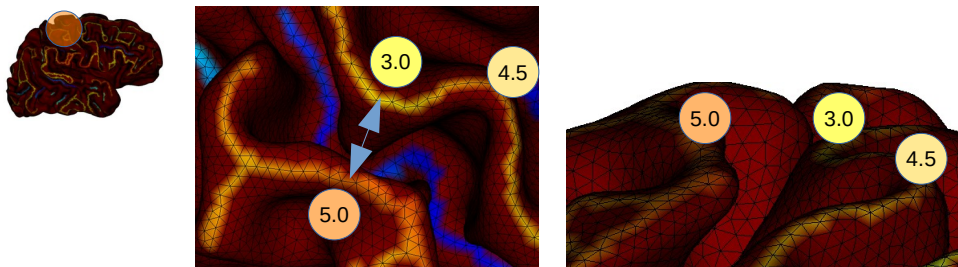
1. The different methods for sulcal depth estimations : diffusion-based: SULC

Crest-to-crest inconsistencies

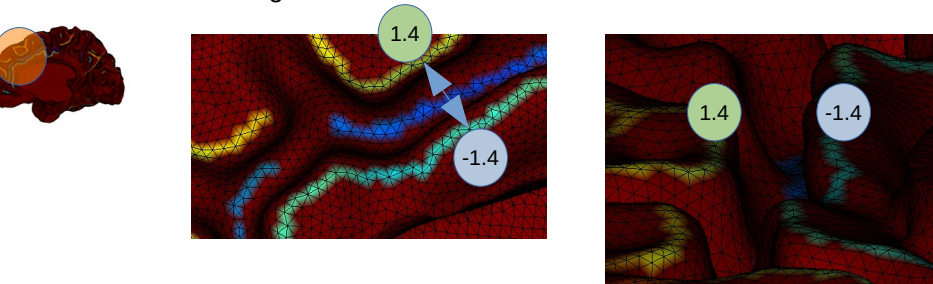
On either side of the sylvian fissure



On either side of the central sulci

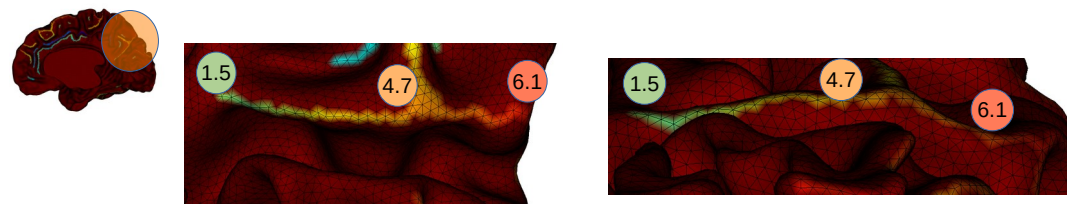


On either side of the cingulate

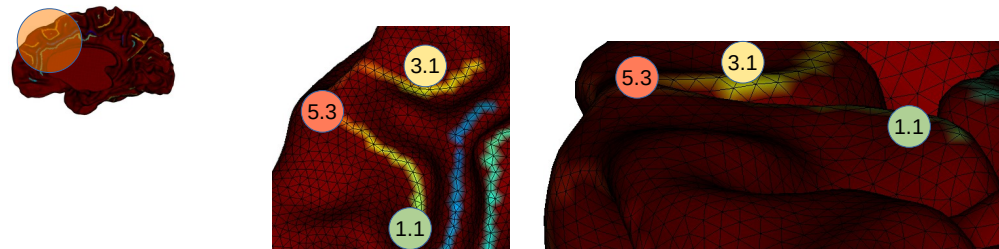


Inconsistencies along a same crest

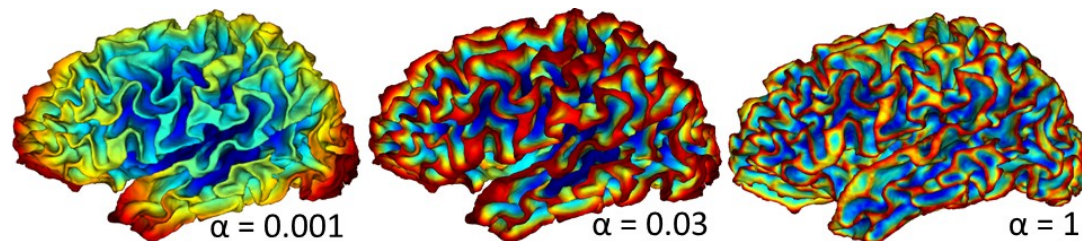
Along the parieto-occipital sulci



along the crests of the medial frontal cortex



the depth potential function



based on a screened Poisson equation :

$$\underbrace{(\alpha \cdot I + \Delta_M)}_{\text{scale control Laplacian}} \underbrace{D_\alpha}_{\text{Depth}} = \underbrace{K}_{\text{Curvature}}$$

~ratio between
curvature and
concavity

~variation of
bending

~bending

$$\begin{aligned} \alpha &: \text{screened coefficient} \quad [\alpha] \equiv L^{-2} \\ I &: \text{Identity matrix} \\ \Delta_M &: \text{Mesh laplacian} \quad [\Delta_M] \equiv L^{-2} \\ K &: \text{Mesh mean Curvature} \quad [K] \equiv L^{-1} \\ D_\alpha &: \text{The DPF} \quad [D_\alpha] \equiv L \end{aligned}$$

Euclidean

- size-dependant external surface
- underestimate convoluted bassins

Geodesic

- size-dependant external surface
- overestimated shallow bassins

Adaptativ

- size-dependant extern surface
- size-dependant discretisation inbetween surface

intuitive

Sulc

- size dependant
- influence of high-concavity regions
- local crest to crest inconsistencies
- global crest to fundi inconsistencies

ready to use

DPF

- size dependant
- empirical setting

- visually promising
- no external surface
- scale parameter

1. What are the different sulcal depth estimation methods ?

2. How to evaluate the different methods ?

3. How deal with size variations ?

2. Evaluate the sulcal depth methods : comparaison

Distance-based method comparaison
value comparaison

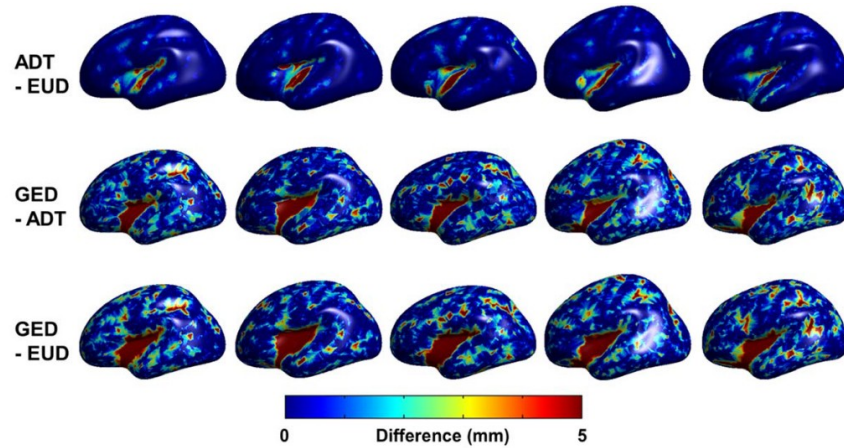
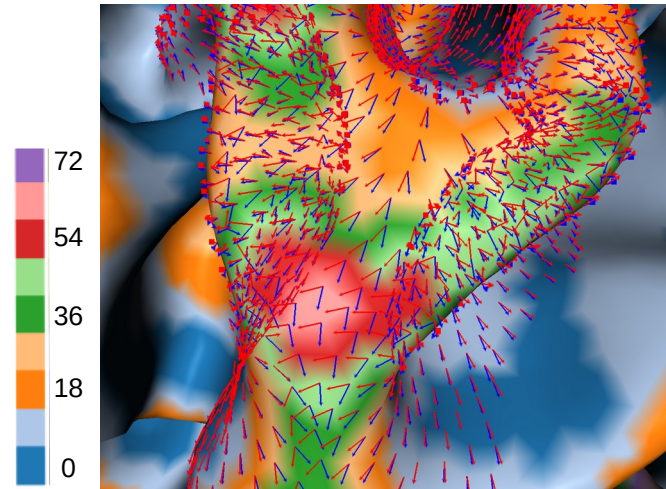
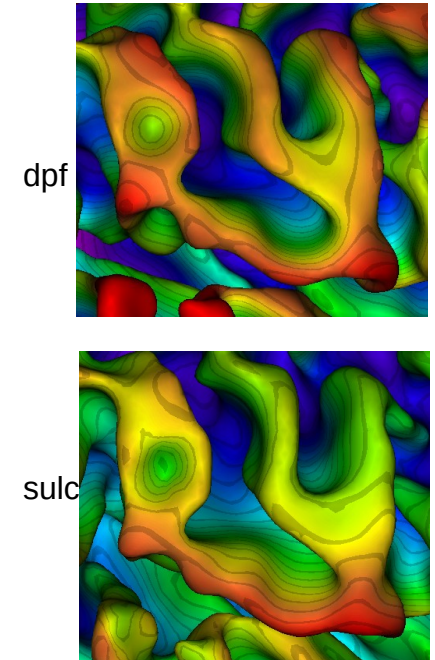


Figure 6. An example of the differences among the algorithms in the 5 subjects.
doi:10.1371/journal.pone.0055977.g006

Diffusion-based method comparaison
gradient comparaison



—▶ dpf
—▶ sulc



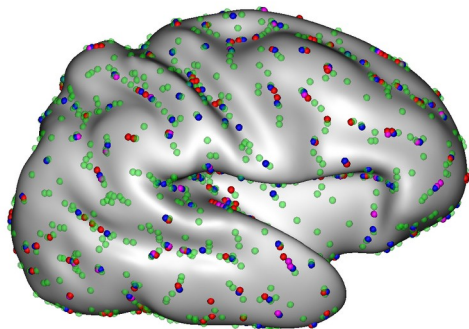
2. Evaluate the sulcal depth methods : comparaison

The difference between methods give **a different interpretation of the surface.**

for exemple :

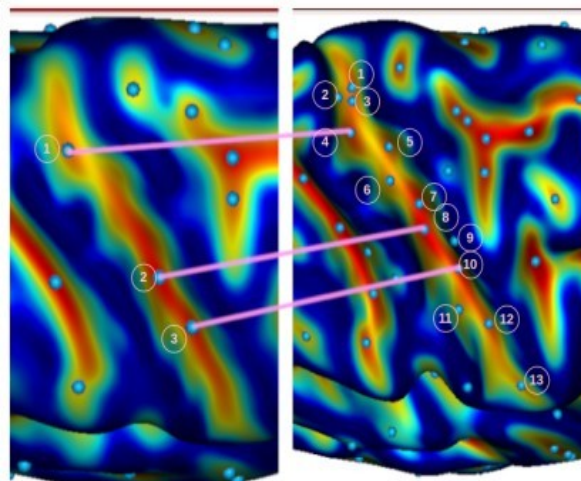
- different scale space

- different spatio temporal emergence of fold :



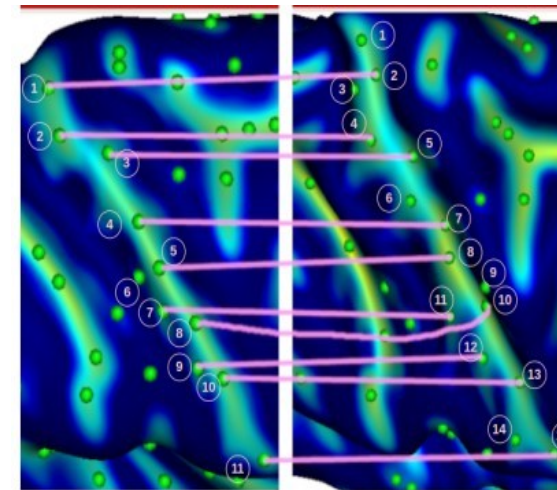
- extrema DPF star , $\alpha_{ref} = 0.03$, $area_{ref} = KKI113$
- extrema DPF basic, $\alpha = 0.03$
- extrema sulc dHCP
- extrema Rusinkievich curv

longitudinal data



dpf setting 1

longitudinal data

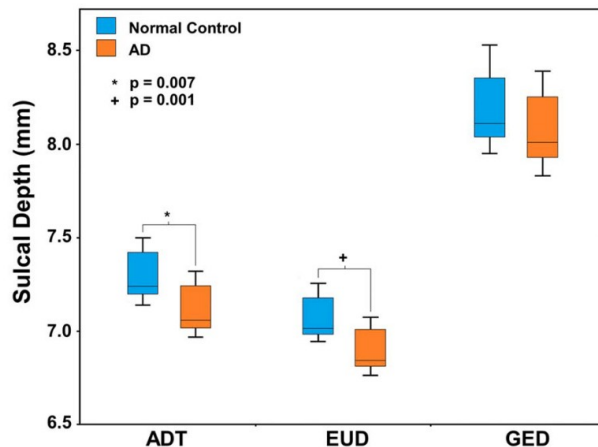


dpf setting 2

2. Evaluate the sulcal depth methods : evaluation in litterature

So far, Methods are evaluate with a clinical application

(Yun et.al, 2013)



Limitations of the actual evaluations:

- Evaluate on an average mesh : do not allow evaluation on a single subject.
- Evaluate with application : the application should not evaluate the measure if you don't have a clear ground truth.

► we need a clear framework for evaluate methods individually without using applications

Define a framework for sulcal depth :

explicit assumptions
on sulcal depth/
biomechanical
model

fold is depletion ?
sulcal roots model ?

Define properties derives
from assumptions

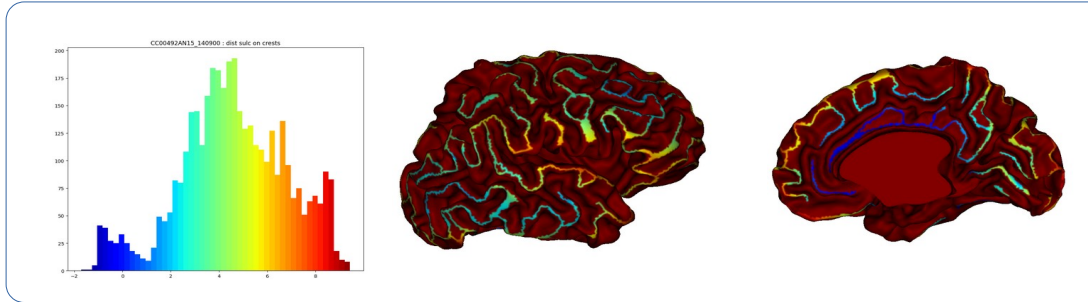
- gyral crest as reference level of depth
- fundi and crest globally separated
- depth direction goes from crest to fundi

Express quantitative
metrics

- ▶ variance of depth on crest
- ▶ median difference between crest and fundi depth
- ▶ angle deviation between gradient and WPs direction

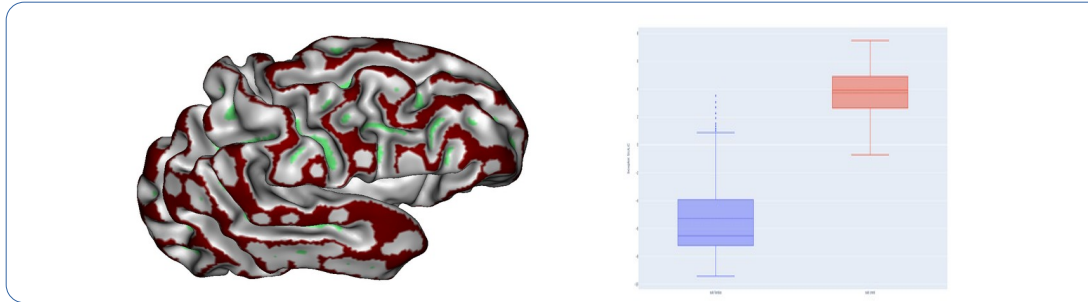
2. Evaluate the sulcal depth methods : contribution : framework

Reference



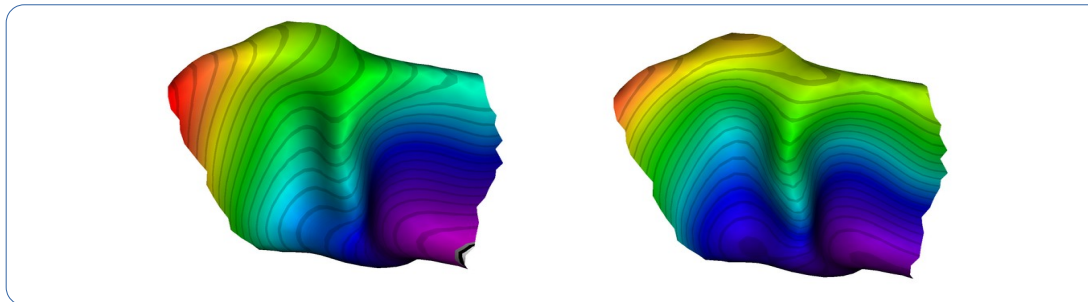
minimise Variance of
depth on crest

Separability



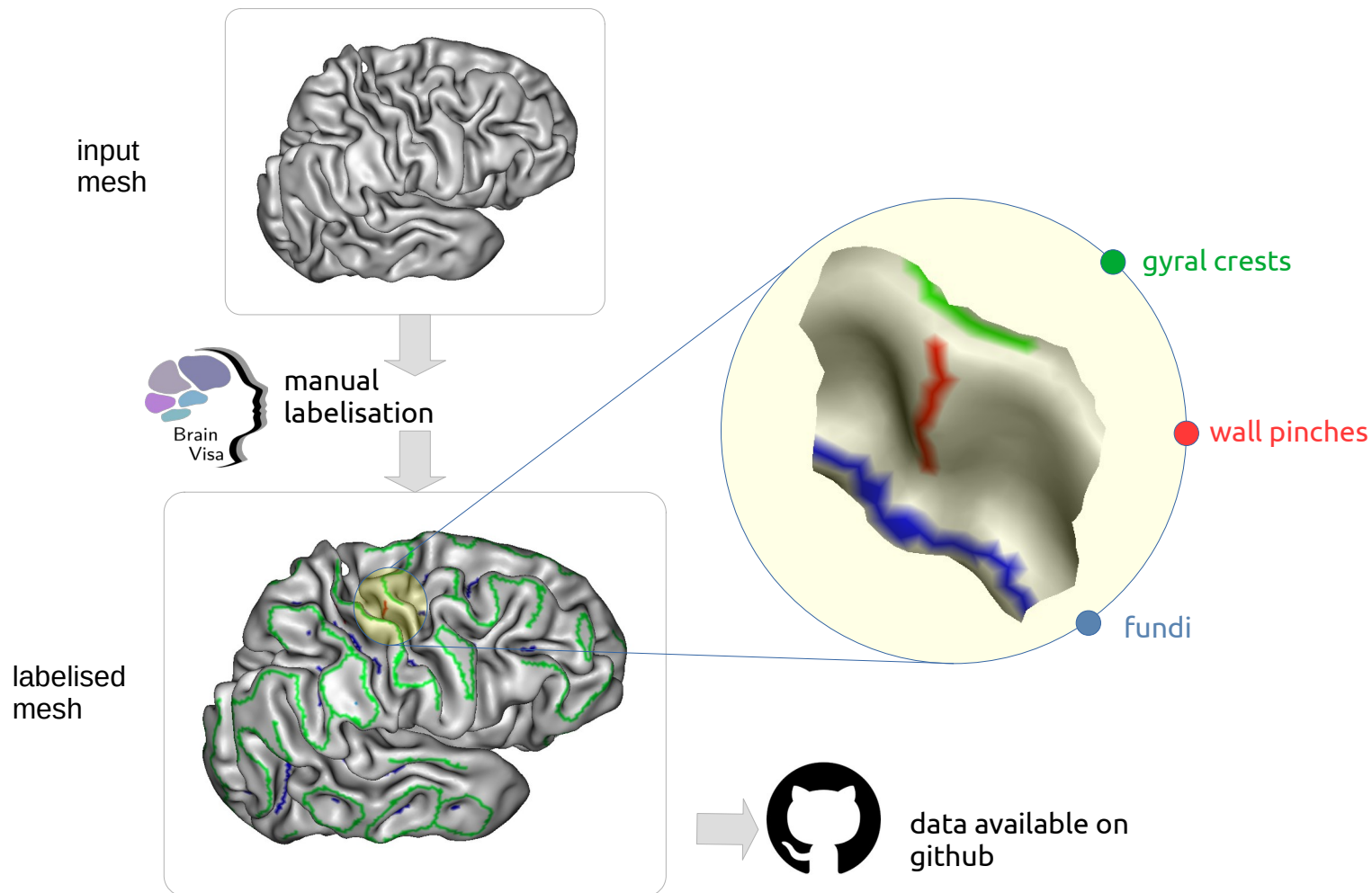
maximise median
between crest and
fundi depth

Direction



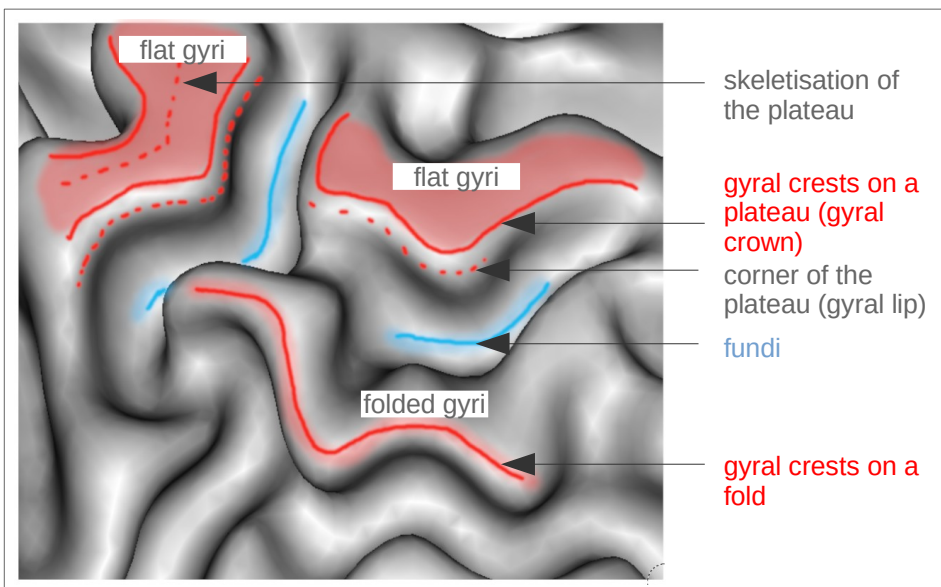
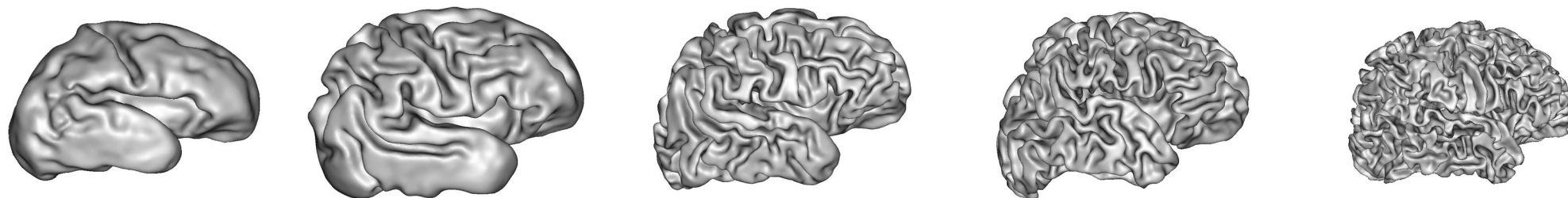
gradient of depth

2. Evaluate the sulcal depth methods : contribution : ground truth



2. Evaluate the sulcal depth methods : contribution : ground truth

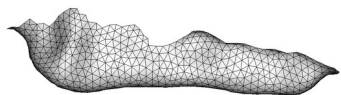
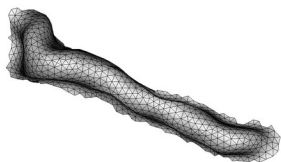
Tracing protocol : 14 dhcp subjects + KKI adult



- **Conservative criteria:** priority is given to reducing the number of false positives rather than improving the number of good positives.
- We define **WPs**, **fundi** and **gyral crests** on a canonical shape of the fold.
- We define the tracing on **variations of the canonical shape**.
- We assess inter-rater reliability.

2. Evaluate the sulcal depth methods : contribution : ground truth

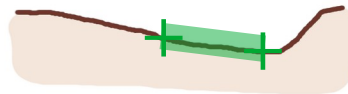
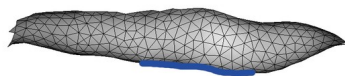
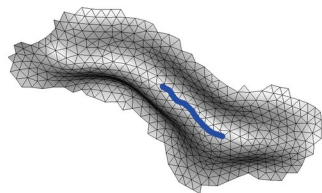
Canonical shape



• inflexion points

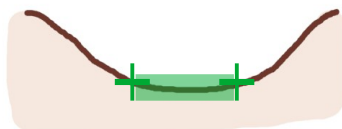
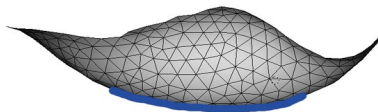
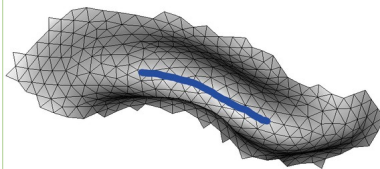
Acceptable variations

one extremity smooth transition



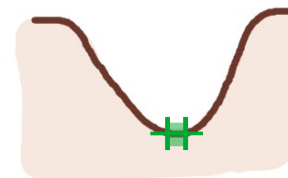
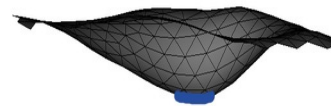
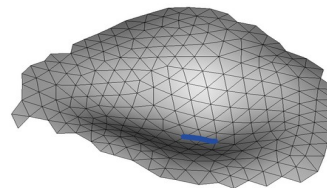
1 inflexions point

U-shape



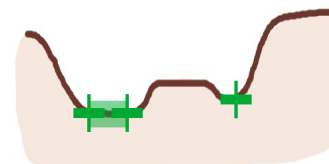
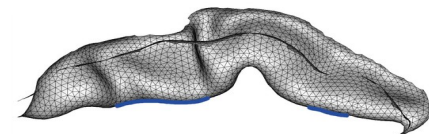
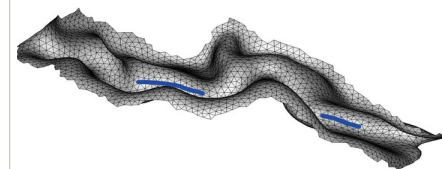
0 inflexions points

Cup-shape



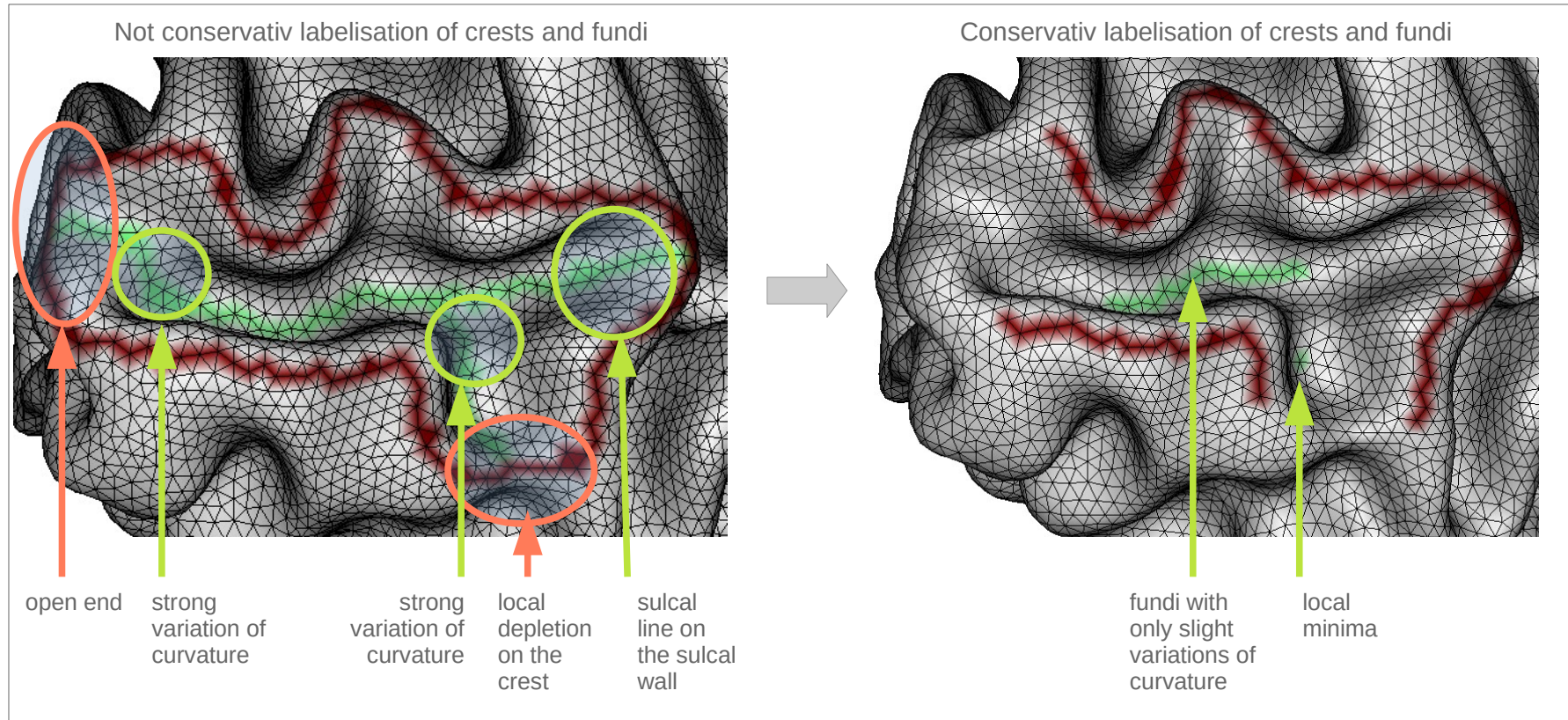
no emergent direction

buried gyri



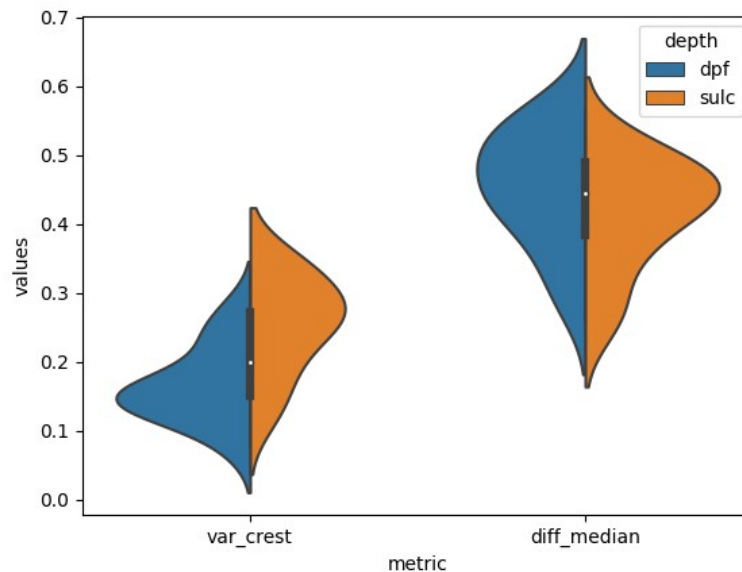
2. Evaluate the sulcal depth methods : contribution : ground truth

conservative criteria



2. Evaluate the sulcal depth methods : contribution : result

comparaison between sulc and DPF with our metrics :



exemple of use :
dpf better than sulc

conclusion :

- initiate common metrics and common framework for evaluate depth
- no need of application
- no need of group analysis
- open data to asses new methods

1. What are the different sulcal depth estimation methods ?
2. How to evaluate the different methods ?

3. How deal with size variations ?

To date, sulcal depth methods are no efficient on young brains

- change methods according the size (ex : curv and apt)
- adapt mannually the methods according size

why this not good :

- artificialy split your data
- need to find an homogeneous space to compare results from different used methods
- circularity of thinking

size independent method is crucial for :

- clarify defintion of depth
- improve reproducibility of results

applications : study on chilhood, neurodevelopmental trajectories, interspecies
comparaison ...

D^* is a size independent depth index

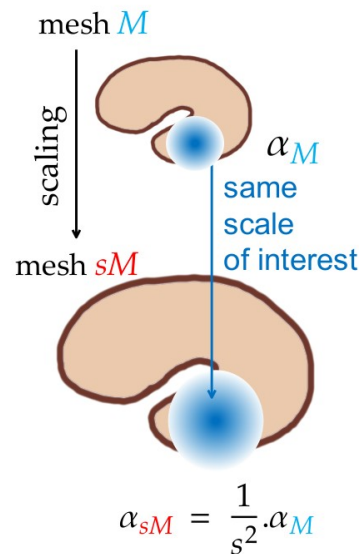
$$D^* = s^{-1} D s^{-2} \alpha$$

normalized Depth scaling Depth scale control

based on the DPF

$$(\alpha \cdot I + \Delta_M) D_\alpha = K$$

scale control Laplacian Depth Curvature



First, we normalize the parameter α to preserve the same scale of interest. Then, we normalise the range of values of the resulting DPF. Proof :

Given the properties of curvature and Laplacian

$K_{sM} = \frac{1}{s} \cdot K_M$ and $\Delta_{sM} = \frac{1}{s^2} \cdot \Delta_M$, we get :

$$(\alpha_{sM} \cdot I + \Delta_{sM}) D_{sM} = K_{sM} \leftrightarrow \left(s \cdot \alpha_{sm} \cdot I + \frac{1}{s} \cdot \Delta_m \right) D_{sM} = K_M$$

$$\text{let set: } \alpha_{sM} = \frac{1}{s^2} \cdot \alpha_M \quad (1), \quad \leftrightarrow \left(\frac{1}{s} \cdot \alpha_M \cdot I + \frac{1}{s} \cdot \Delta_M \right) D_{sM} = K_M$$

$$\text{let set: } D_{sM} = s \cdot D_M \quad (2), \quad \leftrightarrow (\alpha_M \cdot I + \Delta_M) D_M = K_M$$

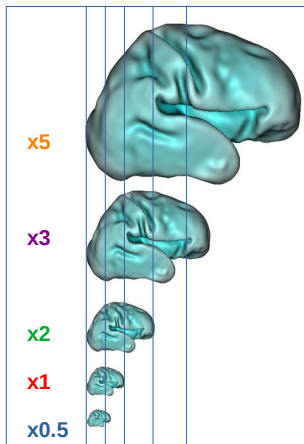
We conclude that (1) and (2) are the two conditions to ensure the normalization of the DPF.

- one coefficient for controlling the scale of interest
- one coefficient for switching between absolut and relativ dept

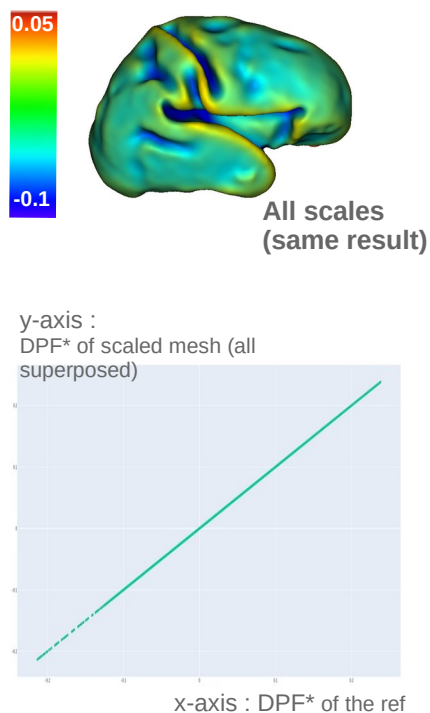
3. deal with size variations : contribution : size-controlled DPF : result

Results

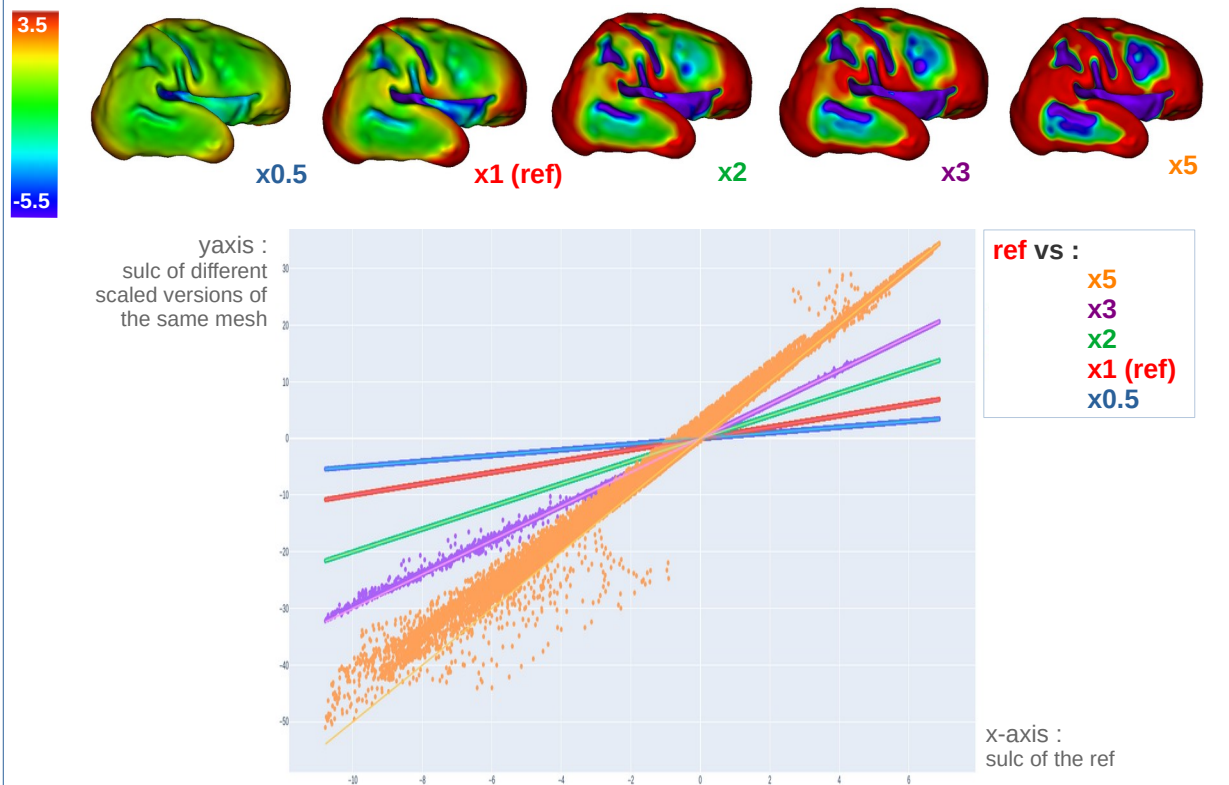
A. Isometric scaling



B. DPF*

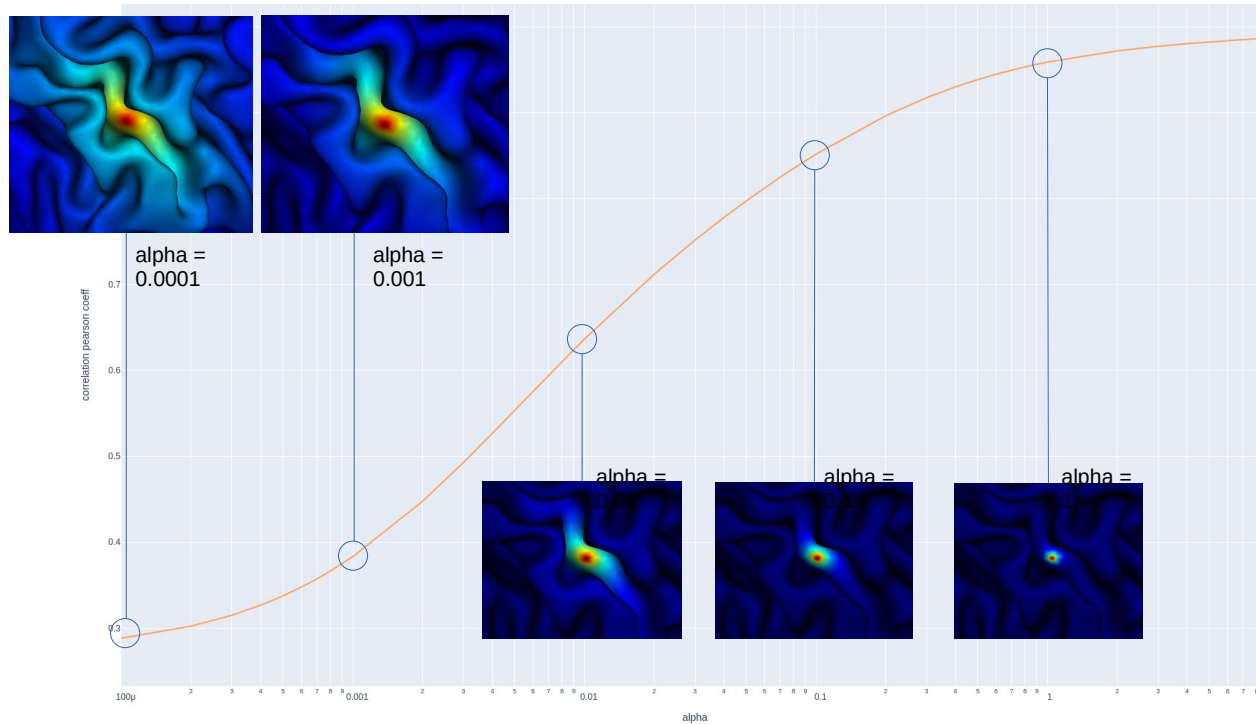


C. sulc from dHCP/freesurfer



3. deal with size variations : contribution : size-controlled DPF

normalisation of the scale parameter : adapt the scale of interest

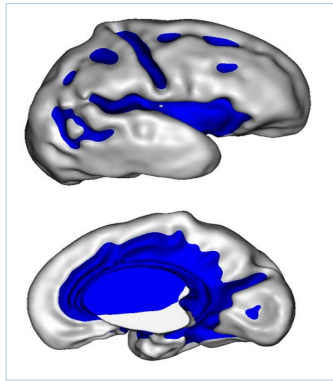


3. deal with size variations : contribution : size-controlled DPF

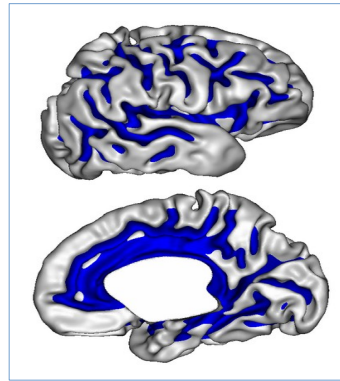
normalisation of the depth : switch between relativ and absolut depth
it exists on unique threshold for detect sulcal bassin whatever the size

Sulc
thresholde
d depth
map

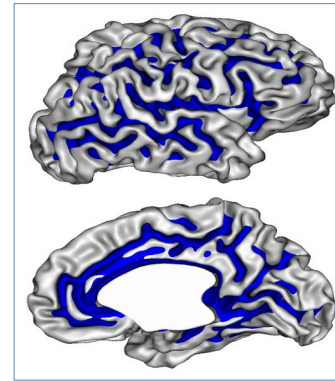
threshold =
T1
for all
subjects



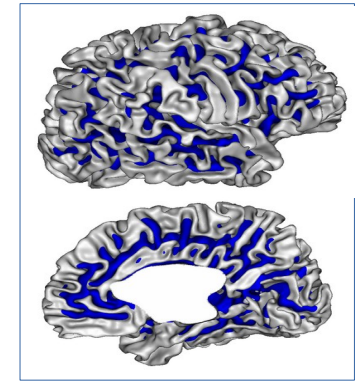
29 weeks



34 weeks



36 weeks

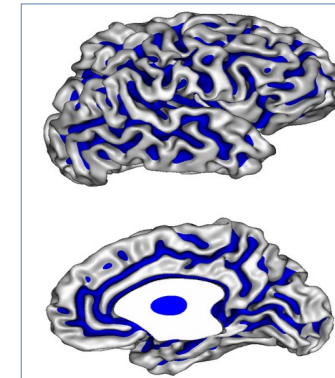
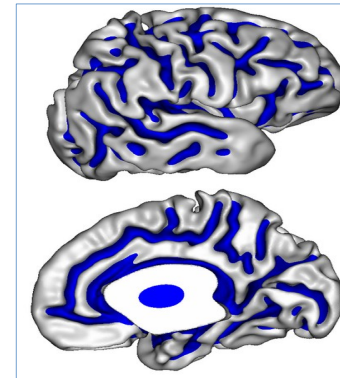
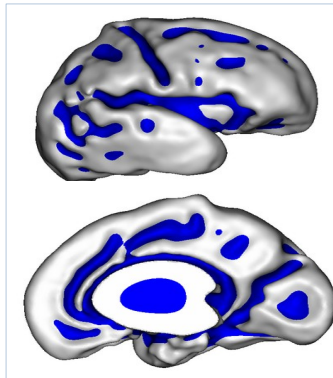


44 weeks

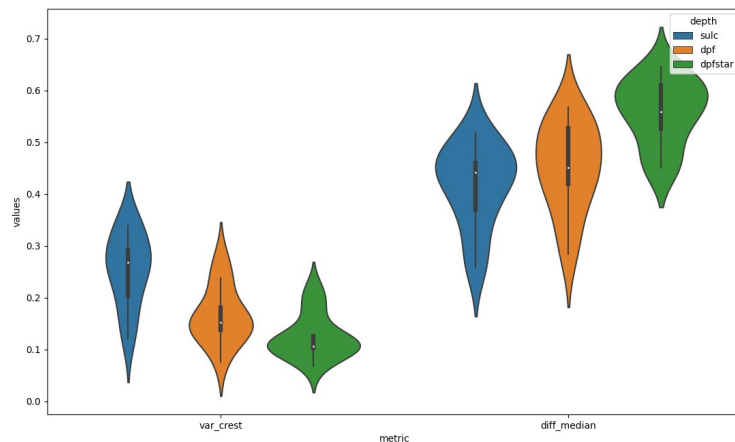
scan age →

DPF*
thresholde
d depth
map

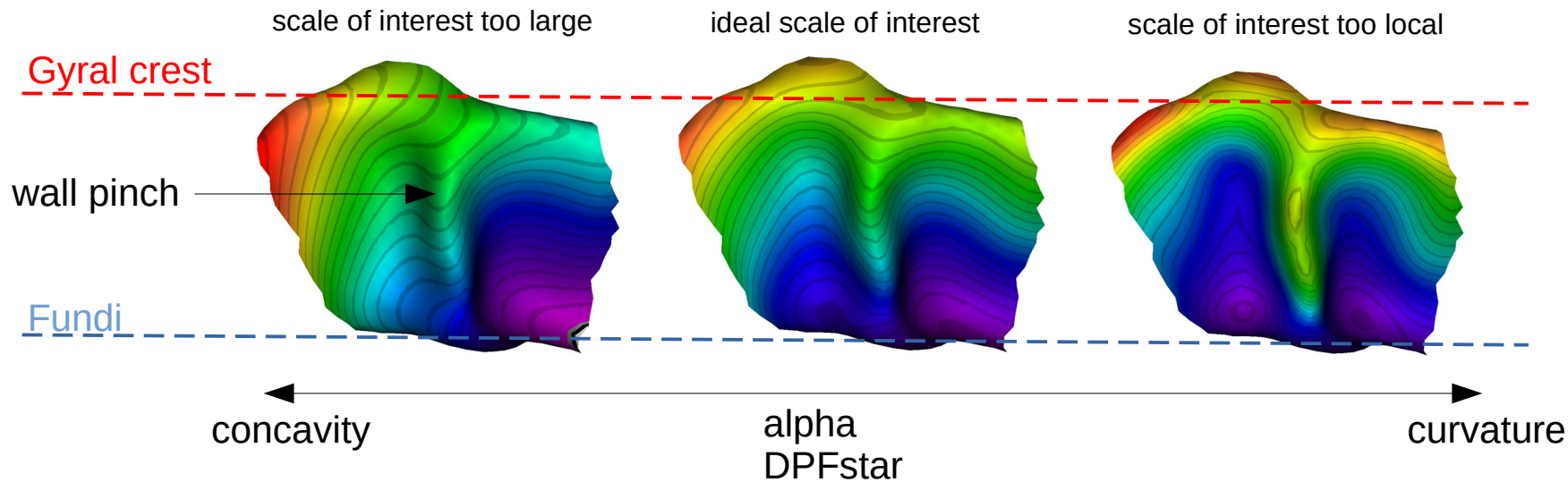
threshold =
T2
for all
subjects

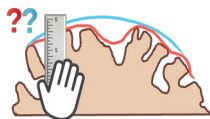


3. deal with size variations : contribution : size-controlled DPF



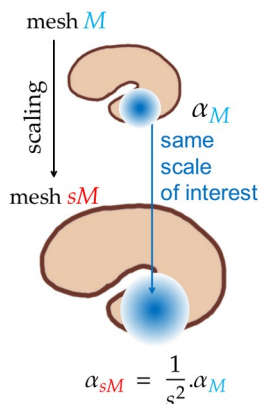
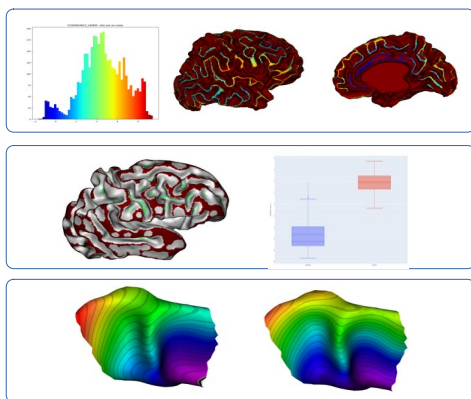
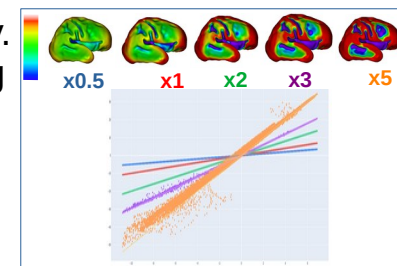
size controlled dpf gives better results than standard dpf !





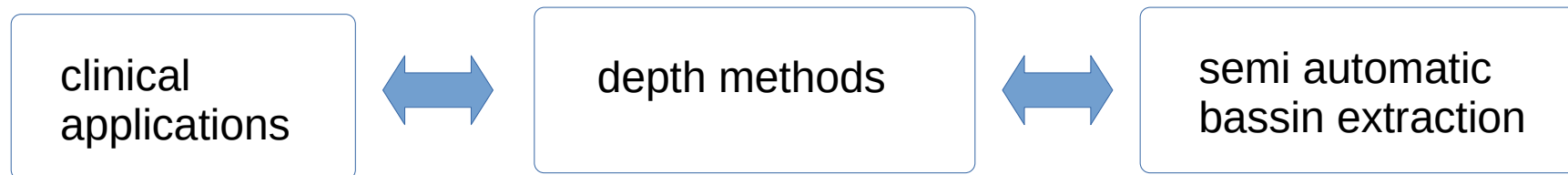
- Although the intuition behind sulcal depth is simple, it's still an **open question** to define a precise way to calculate it.
- Despite the lack of definition, there are several methods for calculating sulcal depth and it appears that sulcal depth is a promising and **relevant morphological feature** for both methodological and clinical applications.

- Distance-based methods require several pre- and post-processing steps that reduce their reliability.
- The widely used sulc method of Freesurfer shows severe spatial incoherences, especially in young brains.
- None of the methods used are easily adaptable to brain size, bringing researchers to use different methods for different sizes.
- Due to the lack of definition, there are no metrics to evaluate sulcal depth methods and this is done so far by evaluating them in terms of clinical applications.

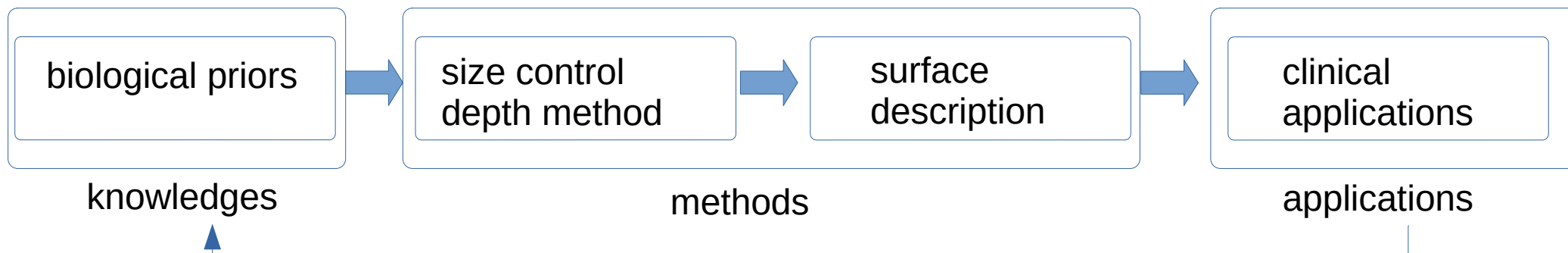


- To address these limitations in depth estimation, we propose to formally adapt the **depth potential function** with a **scale parameter** explicitly expressed as a **function of brain size**.
- And we introduce a **clear and unique framework** that expresses **properties for depth** derived from biological priors and allows quantitative evaluation without group analysis and relative comparisons.
- Our method gives **better results** than SULC.

before : not a good practice for open science



After: a better practice for open science



- equation can be upgraded regarding your biological priors
- allow community to improve the methods when knowledges improve
- allow to build method on the same basement

Theory : A very flexible equation

- improve the isometric scaling with an allometric scaling
- add constraint terms

Practice : analyse spatial distribution and temporal emergence for early malformation detections

- improve reliability of sulcal pits extraction algorithm (Auzias et al, 2015)
- use sulcal pit extraction method to improve the Multimodal Surface Matching algorithm (Robinson et al. 2014)
- to generate cortical surface templates at each week of gestation between 20 and 40 weeks.

These new tools will allow me to assess the spatial distribution and temporal emergence of sulcal roots to characterise folding dynamics in healthy and malformed fetuses.

use the fetal MRI database acquired at the Timone Hospital as part of routine clinical practice, built in parallel with my thesis :

- 560 MRI scans of fetuses with no abnormalities,
- 90 fetuses with agenesis of the corpus callosum
- 20 fetuses with cerebral malformations such as microcephaly, macrocephaly or polymicrogyria.

Thanks,